

# A PID Controller For Lego Mindstorms Robots

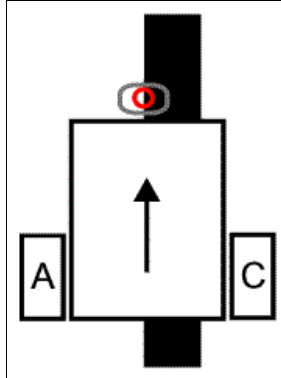
A **PID Controller** is a common technique used to control a wide variety of machinery including vehicles, robots and even rockets. The complete mathematical description of a PID Controller is fairly complex but a much simpler understanding is really all that is needed to use a PID effectively.

This document is a description of how to create a PID Controller for use with Lego Mindstorms Robots using the NXT-G programming language.

It will be easier if we have an actual task in mind so I will describe how to create a PID to do line following. Once created, the same PID can be used, with only minor modifications, with any other Mindstorms application such as getting a robot that can drive as straight as possible, or even for a robot that can balance with nothing but 2 wheels touching the ground like a Segway.

A PID is really pretty straight forward and the typical description of a PID is easily understood by anyone that has had Calculus. This document is targeted towards First Lego League kids in third through eighth grade. *Since there aren't many kids that have had Calculus I'll try to build the whole concept up from a very simple starting point without using any Calculus.*

So lets start with the basic layout of a robot that would be suitable for line following. At the right is a simplified drawing of a top view of the robot with all the details we need. The robot is a differential steer robot with two motors, each connected to one of the wheels A and C. The robot has a light sensor mounted at the front that points straight down so it sees nothing but the mat (floor, ground, table top, whatever the robot is on). The red circle represents the fairly small spot on the mat that the light sensor can actually "see". The rest of the large rectangle with an arrow, the arrow shows the normal direction of travel.

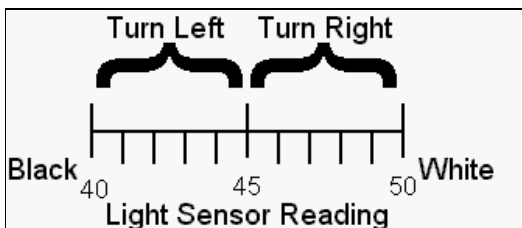


Our goal is to get the robot to follow the fat black line. Line following is a basic robotic behavior and is often one of the first things people learn. A mobile device that can follow a line displays all the characteristics of a true robot. It uses sensor to gather information about the world around it and changes it's behavior depending upon that information.

Line followers can be built with one light sensor, or two, or a dozen or however many you happen to have. In general, the more light sensors you have the better you can follow a line. Here we'll limit ourselves to a single Mindstorms light sensor. Even with a single sensor we should be able to build a robot that can track the line very precisely even if the line has curves in it. The thing you usually loose with a single sensor is the ability to follow the line while moving fast. Often, the more sensors you have the faster the robot can move while it follows the line.

The first trick we'll use, which is unrelated to a PID, is that we won't try to actually follow the line. Instead, we'll try to follow the edge of the line. Why? Because if we follow the line itself (the black) then when the robot drifts off the line and the sensor "sees white" we don't know which side of the line we are on. Are we left or right of the line? If we follow the line's edge then we can tell which way we are off the edge as the robot drifts off the line. If the light sensor "sees white" then we know it is left of the line's edge (and the line). If it "sees black" then we know it is to the right of the line's edge (and on the line). This is called a *"left hand line follower"* since it is following the line's left edge.

We need to know what values the light sensor returns when it "sees white" and when it "sees black". A typical uncalibrated sensor might give a "white" reading of 50 and a "black" reading of 40 (uncalibrated, on a 0 to 100 scale). It is convenient to draw the values on a simple number line to help visualize how we *convert light sensor values into changes in the robot's movement*. Below are our made up light values for white and black.

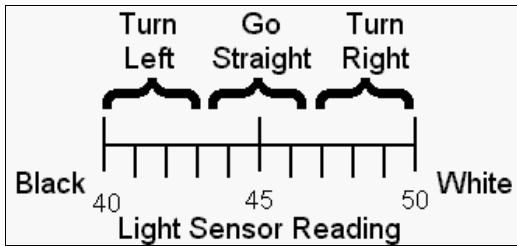


We'll just divide the range into two equal pieces and say that if the light level is less than 45 we want the robot to turn left. If it is greater than 45 we want to turn right. I won't go into how exactly the turns should be done. I'll just say that gentle turns work well for a fairly straight line. A line with lots of curves usually needs to be making sharper turns. For gentle turns you might use Power levels of 50% on the fast wheel and 20% on the slow wheel. For sharper turns on a curvy line you might need to use 30% power for the fast wheel and coast or brake the slow wheel. Whatever power levels you use the numbers will be the same for the two turns, you just switch which motor gets the big number and which get the smaller number (or a stop command).

This type of a line follower will follow a line but it isn't very pretty. It looks OK on a straight line with with the motors programmed for gentle turns. But if the line has any curves then you have tell the robot to use sharper turns to follow line. That makes the robot swing back and forth across the line. The robot only "knows" how to do two things; turn left and turn right. This approach can be made to work but it is not very fast or accurate and looks terrible.

In the above approach the robot never drives straight, even if it is perfectly aligned with line's edge and the line is straight. That doesn't seem very efficient does it?

Lets try to fix that. Instead of dividing our light value number line into two regions lets divide it into three.



So now if the light level is less than 43 we want the robot to turn left. If the light value is between 44 and 47 we want it to go straight (zoom zoom). If the light level is greater than 47 we want to turn right. This can be easily be implemented in Mindstorms NXT-G with a switch (yes/no) within a switch. You actually only have to do two tests not three.

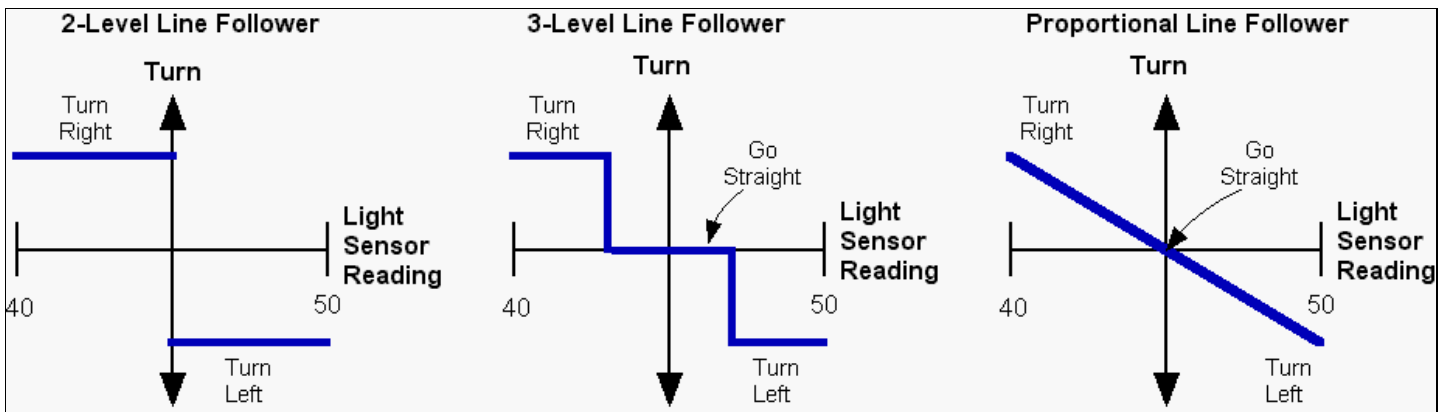
This approach works better than the first one. At least now the robot is *sometimes* moving straight forward. As with the first approach you still have to decide what kinds of turns you need and that usually depends on the characteristics of the line you are following. The robot will probably still hunt back a forth a fair amount.

The astute reader will probably have thought "*well if three light ranges are better than two than what about adding even more?*" That is the beginning of a PID.

### The "P" in "PID": Proportion(al) is the key

So what will happen if we add more divisions to our light scale line? Well the first thing we have to deal with is what does "turn" mean with more than three light ranges? In our first approach the robot could do just two things, turn left or right. The turns were always the same just in opposite directions. In the second approach we added the "go straight" to the two turns. If we have more than three ranges then we need more "kinds" of turns.

To help understand "more kinds of turns" we will redo or number line a bit and convert it into a graph. Our X-axis (horizontal) will be our light values just like on the number lines. The Y-axis (vertical) will be our "turn" axis.



On the left is our original two level setup expressed on a graph. The robot can only do two things (shown by the blue lines), turn right or left and the turns are always the same except for their direction. In the center is the three level follower. The added center range is where the robot drives straight (Turn=0). The turns are the same as before. On the right is a **Proportional** line follower. In a proportional line follower the turn varies smoothly between two limits. If the light sensor reading says we are close to the line then we do a small turn. If we are far from the line then we do a big turn. Proportional is an important concept. Proportional means there is a linear relationship between two variables. To put it even simpler, proportional means a graph of the variables against each other produces a straight line (as in the right hand graph above).

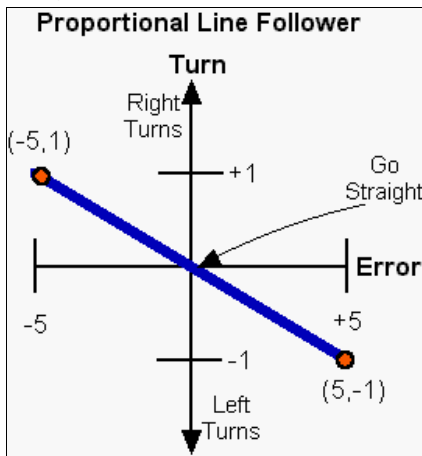
As you may know, the equation of a straight line is:

$$y = mx + b$$

Where y is the distance up (or down) the Y-axis, x the distance on the X-axis, m is the slope of the line and b is the Y intercept, the point where the line crosses the Y-axis when x is zero. The slope of the line is defined as the change in the y value divided by the change in the x value using any pair of points on the line.

If you don't know much about lines (or have forgotten what you once new) I'll expand a bit

and make some simplifications to our graph and equation. First, we will shift the center of our light number line (the X-axis) to zero. That's easy to do. For our 40 and 50 light value range we just subtract 45 (that's the average of 40 and 50,  $(40+50)/2$ ) from all of our light readings. We will call that result the **error**. So, if the light value is 47 we subtract 45 and get an **error**=2. The **error** tells us how far off the line's edge we are. If the light sensor is exactly on the line's edge our **error** is zero since the light value is 45 and we subtract 45 from all of our readings. If the sensor is all the way out into the white our **error** is +5. All the way into the black the **error** is -5.



In the above graph I have shifted the axis by converting it to an error scale. Since the line now crosses the Y-axis at zero that means b is zero and the equation for the line is a bit simpler;

$$y = mx$$

or using our labels

$$\text{Turn} = m \cdot \text{error}$$

We haven't yet defined what the turn axis means so for now we will just say the turns range from -1 (hard turn to the left) to +1 (hard turn to the right) and a zero turn means we are going straight. The slope of the line in the graph above can be calculated using the two points marked in red (any two points on the line will work);

$$\text{slope} = m = (\text{change in } y) / (\text{change in } x) = (1 - (-1)) / (-5 - 5) = 2 / -10 = -0.2$$

The slope is a **proportionality constant** and is the factor that you have to multiply the **error** (x value) by to convert it into a **Turn** (y value). That's an important thing to remember.

The "slope" has a couple names that all mean the same thing, at least in this context. In the PID literature slopes (proportionality constants, m in the equation of a line) are called "**K**" (from misspelling of the word "constant"?). Various **Ks** show up all over the PID literature and are a very important. You can think of a **K** (or m or slope or proportionality constant) as a *conversion factor*. You use **K** to convert a number that means one thing (light values or error in our case) into something else like a turn. That's all that a **K** does. Very simple and very powerful.

So using these new names for our variables the equation of the line is;

$$\text{Turn} = K \cdot (\text{error})$$

In words that's "take the **error** and multiply it by the proportionality constant **K** to get the needed turn. The value **Turn** is the output of our P controller and is called the "**P term**" since this is only a proportional controller.

You may have noticed that in the last graph the line does not extend outside the **error** range of -5 to +5. Outside the range of -5 to +5 we can't tell how far the sensor is from the line. All "white" looks the same once the sensor can't see any black at all. Remember that this range is arbitrary, your range will be determined by your light sensor setup, the colors of the mat etc. Once the light sensor gets too far from the line edge it starts to give a constant reading, that means the light sensor reading is no longer proportional to the **error**. We can only judge how far the sensor is from the line's edge when the sensor is actually pretty close to it. Over that narrow range the light sensor reading is proportional to the distance. So our sensor setup has a limited range over which it gives proportional information. Outside that range it tells us the correct direction but the magnitude (size) is wrong. The light sensor reading, or the **error**, is smaller than it should be and doesn't give as good an idea of what the turn should be to fix the **error**.

In the PID literature the range over which the sensor gives a proportional response is called the "**proportional range**" (go figure :D ). The proportional range is another very important concept in PIDs. In our line follower the proportional range for the light sensor is 40 to 50, for the **error** it is -5 to +5. Our motors also have a proportional range, from -100 (full power backwards) to +100 (full power forwards). I'll just say a couple things about the importance of the proportional range:

(1) You want the proportional range to be as wide as possible. Our light sensor's proportional range is pretty small, that is, the sensor has to be pretty close to the line edge to get proportional information. Exactly how wide the range is depends mostly on how high the sensor is above the mat. If the sensor is very close to the mat, say 1/16 inch, then the sensor is seeing a very small circle on the mat. A small side to side movement of the light sensor will swing the **error** from -5 to +5, that's all the way through our proportional range. You might say the sensor has "tunnel vision" and it can only see a very small part of the mat. The sensor has to be very close to the line edge to get a reading that isn't either "white" or "black". If the sensor is moved higher off the mat then it sees a larger circle on the mat. At a height of about 1/2 inch the light sensor appears to be looking at a circle on the mat that is about 1/2 inch across. With the sensor up this high the proportional range is much wider, since the light sensor only needs to stay within +/- 1/2 inch of the line edge to maintain a proportional output. Unfortunately, there are two drawbacks to a high light sensor. First, a high light sensor "sees", and responds to, the room lights much more than a low sensor. A high sensor also has less difference between black and white than a low sensor. At a sufficiently large distance black and white will give the same reading.

(2) Outside the proportional range the controller will move things in the correct direction but it will tend to under correct. The controller's proportional response is limited by the proportional range.

### From P to actual motor power levels

How can we implement the turns? What should the actual motor power levels be? One way to do the turns is to define a "Target power level", which I'll call "**Tp**". Tp is the power level of both motors when the robot is supposed to go straight ahead, which it does when the error=0. When the **error** is not zero we use the equation **Turn = K\*(error)** to calculate how to change the power levels for the two motors. One motor will get a power level of **Tp+Turn**, the other motor will get a power level of **Tp-Turn**. Note that since our **error** is -5 to +5 that means **Turn** can be either positive or negative which corresponds to turns in opposite directions. It turns out that that is exactly what we want since it will automatically set the correct motor as the fast motor and the other one as the slow motor. One motor (we'll assume it is the motor on the left of the robot plugged into port A) will always get the **Tp+Turn** value as it's power level. The other motor (right side of robot, port C) will always get **Tp-Turn** as it's power level. If **error** is positive then **Turn** is positive and **Tp+Turn** is greater than **Tp** and the left motor speeds up while the right motor slows down. If the **error** changes sign and becomes negative (meaning we have crossed over the line's edge and are "seeing black") then **Tp+Turn** is now less than **Tp** and the left motor slows down and the right motor speeds up since **Tp-Turn** is greater than **Tp**. (Remember that the negative of a negative is a positive). Simple eh? Hopefully it'll be a bit clearer as we go on.

### Pseudo Code for a P Controller

First we need to measure the values the light sensor returns for white and black. From those two numbers we can calculate the **offset**, that is, how much to subtract from a raw light reading to convert it to an **error** value. The **offset** is just the average of the white and black readings. For simplicity I'll assume that the **offset** has already been measured and stored in a variable called **offset**. (A nice upgrade would be to have the robot measure the white and black levels and calculate the **offset**.)

We will also need a storage location for the **K** constant, we'll call that **Kp** (the **K**onstant for the **p**roportional controller). And, an initial guess as to what **Kp** should be. There are a lot of ways to get that first **Kp** value. You can guess and then refine it by trial and error. Or, you can try to estimate a value based on the characteristics of the sensor and robot. We'll do the latter. We will use a **Tp** (target power) of 50, when the error is zero both motors will run at power level 50. The error ranges from -5 to +5. We'll guess that we want the power to go from 50 to 0 when the error goes from 0 to -5. That means the **Kp** (the slope remember, the change in y divided by the change in x) is;

$$Kp = (0 - 50)/(-5 - 0) = 10.$$

We will use the **Kp=10** value to convert an **error** value into a **turn** value. In words our conversion is "for every 1 unit change in the **error** we will increase the power of one motor by 10". The other motor's power gets decreased by 10.

So, in pseudo code ("pseudo code" means this isn't actual NXT-G, or any other type of program code, instead it is just a detailed listing of what we want the program to do):

```

Kp = 10                                ! Initialize our three variables
offset = 45
Tp = 50
Loop forever
  LightValue = read light sensor        ! what is the current light reading?
  error = LightValue - offset           ! calculate the error by subtracting the offset
  Turn = Kp * error                    ! the "P term", how much we want to change the motors' power
  powerA = Tp + Turn                   ! the power level for the A motor
  powerC = Tp - Turn                   ! the power level for the C motor
  MOTOR A direction=forward power=powerA ! issue the command with the new power level in a MOTOR block
  MOTOR C direction=forward power=powerC ! same for the other motor but using the other power level
end loop forever                       ! done with this loop, go back to the beginning and do it again

```

That's it, well almost. There is a subtle problem that should be corrected. But give it a try anyway. If your robot appears to avoid the line edge, instead of trying to find it, the most likely cause is that you have swapped the turn directions. Change **Kp** to -10 and see what happens. If that fixes the turn directions then change **Kp** back to +10 and change the signs

in the two power lines to;

```
powerA = Tp - Turn
powerC = Tp + Turn
```

There are two "tunable parameters" and one constant in this P controller. The constant is the **offset** value (the average of white and black light sensor readings). You'll need to write a short program to measure the light levels on your mat with your robot. You need a "black" and a "white" value. Calculate the average and put it into the P controller program in the **offset** variable. Almost all line followers require that you (or code written by you and executed by the robot) do this step.

The **Kp** value and the target power **Tp** are the tunable parameters. A tunable parameter has to be determined by trial and error. **Kp** controls how fast the controller will try to get back to the line edge when it has drifted away from it. **Tp** controls how fast the robot is moving along the line.

If the line is pretty straight you can use a large **Tp** to get the robot running at high speed and a small **Kp** so the turns (corrections) are gentle.

If the line has curves, especially sharp ones, there will be a maximum **Tp** value that will work. If **Tp** is bigger than that maximum it won't matter what **Kp** is, the robot will lose the line when it encounters a curve because it is moving too fast. If **Tp** is really small then almost any **Kp** value will work since the robot will be moving very slowly. The goal is to get the robot moving as fast as possible while still being able to follow the line of interest.

We had guesstimated a starting value for **Kp** of 10. For **Tp** you might start at even lower than suggested above, perhaps 15 (the robot will be moving pretty slow). Try it and see how it works. If you lose the line because the robot seems to turn sluggishly then increase **Kp** by a couple and try again. If you lose the line because the robot seems hyperactive in hunting back and forth for the line then decrease **Kp**. If the robot seems to follow the line pretty well then increase **Tp** and see if you can follow the line at the faster speed. For each new **Tp** you will need to determine a new **Kp**, though **Kp** usually won't change too much.

Following a straight line is usually pretty easy. Following a line with gentle curves is a bit harder. Following a line with sharp curves is the hardest. If the robot is moving slow enough then almost any line can be followed, even with a very basic controller. We want to get good line following, good speed and the ability to handle gentle corners. (Lines with sharp corners usually take more specialized line followers.)

It is likely that the best P controller will be different for each kind of line (line width, sharpness of curves etc.) and for different robots. In other words, a P controller (or a PID controller for that matter) is tuned for a particular kind of line and robot and will not necessarily work well for other lines or robots. The code will work for many robots (and many tasks) but the parameters, **Kp**, **Tp** and **offset**, have to be tuned for each robot and each application.

### Doing math on a computer that doesn't know what a decimal point is causes some problems

**NOTE:** This work was done using NXT-G version 1.1 which only supports integers. NXT-G version 2 supports floating point numbers so the following may not be needed if you have version 2 or later.

In the process of tuning the P controller you will be tweaking the **Kp** value up and down. The expected range of values that **Kp** might depend on exactly what the P controller is doing. How big is the input range and how big is the output range? For our line follower P controller the input range is about 5 light units, and the output range is 100 power units, so it seems likely that **Kp** will be in the vicinity of  $100/5=20$ . In some cases the expected **Kp** won't be that big. What happens if the expected **Kp** is one? Since variables in NXT-G are limited to integers, when you try to tune the **Kp** value all you can try is ...-2, -1, 0, 1, 2, 3, ... . You can't enter 1.3 so you can't try **Kp**=1.3. You can't use any number with a decimal point! But there will probably be a large difference in the robot behavior when you change the **Kp** by the smallest possible change of 1 to 2. With **Kp**=2 the robot tries twice as hard to correct the error compared to **Kp**=1. The motor power level changes twice as much for the same change in the light levels. We really would like to have finer control of **Kp**.

It is pretty easy to fix this problem. All we will do is multiply the **Kp** by a power of ten to increase the useable range within the integer restriction. If it is expected that **Kp** might be near 1 then a value of 100 as the multiplier would be a good bet. Indeed, it is probably best to just go ahead and always use  $100 \cdot Kp$  as the number you actually enter into the program. Once **Kp** has been multiplied by 100 we can now enter what would have been 1.3 as 130. 130 has no decimal point so NXT-G is happy with the number.

But doesn't that trash the calculation? Yes it does but it is easy to fix. Once we have calculated the P term we will divide by 100 to remove our multiplier. Remember our equation that defines the P controller from earlier;

$$\text{Turn} = Kp \cdot (\text{error})$$

We will multiply **Kp** by 100, which means our calculated **Turn** is 100 times bigger than it should be. Before we use **Turn** we must divide it by 100 to fix that.

So, our new and improved pseudo code for a line following P controller is:

```

Kp = 1000 ! REMEMBER we are using Kp*100 so this is really 10 !
offset = 45 ! Initialize the other two variables
Tp = 50
Loop forever
  LightValue = read light sensor ! what is the current light reading?
  error = LightValue - offset ! calculate the error by subtracting the offset
  Turn = Kp * error ! the "P term", how much we want to change the motors' power
  Turn = Turn/100 ! REMEMBER to undo the affect of the factor of 100 in Kp !
  powerA = Tp + Turn ! the power level for the A motor
  powerC = Tp - Turn ! the power level for the C motor
  MOTOR A direction=forward power=powerA ! actually issue the command in a MOTOR block
  MOTOR C direction=forward power=powerC ! same for the other motor but using the other power level
end loop forever ! done with loop, go back and do it again.

```

### Wait, what was the "Subtle Problem" you mentioned with the first version of the P controller?

There are always subtle problems. Sometime they matter and sometimes they don't. ;)

In this case, one problem is that when we calculate the motor power level (e.g.,  $powerC = Tp - Turn$ ) it is possible to get a negative number for the power. We want a negative number to mean that the motor should reverse direction. But the data port on a NXT-G MOTOR block doesn't understand that. The power level is always a number between 0 and +100. The motor's direction is controlled by a different input port. To get the motor to react correctly when the power is negative you'll need to handle it in the program. Here is one way to do that:

```

If powerA > 0 then ! positive motor power is no problem
  MOTOR A direction=forward power=powerA
else
  powerA = powerA * (-1) ! negative motor power needs to be made into
  MOTOR A direction=reverse power=powerA ! a positive number and the motor direction
end If ! needs to be reversed on the control panel

```

The MOTOR block receives the power (powerA for the A motor) via a data wire. The direction is set with the check boxes in the motor's parameter window.

You will need a similar chunk of code for the C motor. Now when the calculated power goes negative the motors will be properly controlled. One thing this does is allow the P controller to go all the way to a "zero turning radius turn" and the robot can spin in place if needed. Of course, that may not actually help.

There are a couple other things that might be subtle problems. What happens when you send a power level that is greater than 100 to the motor? It turns out that the motor just treats the number as 100. That is good for the program but not the best thing to have happen in a P (or PID) controller. You would really prefer that the controller never tries to ask the motors to do something they can't. If the requested power isn't too far above 100 (or below -100) then you are probably OK. If the requested power is a lot bigger than 100 (or a lot less than -100) then it often means the controller is spiraling out of control. So, make sure you have a fire extinguisher handy!

### P Controller Summary

Hopefully you've picked up enough to understand a P (proportional) controller. It is pretty simple. Use a sensor to measure something that you are trying to control. Convert that measurement to an **error**. For the line follower we did that by subtracting the average of black and white light values. Multiply the **error** by a scaling factor called **Kp**. The result is a correction for the system. In our line follower example the correction is applied as an increase/decrease in the power level of the motors. The scaling factor **Kp** is determined using a bit of educated guessing and then fine tuned by trial and error.

P controllers can handle a surprising wide range of control problems, not just following a line with a Lego robot. In general, P controllers work very well when a few conditions are met.

1. The sensor needs to have wide dynamic range (which unfortunately is not true for our line following robot).
2. The thing being controlled (motors in our case) should also have a wide dynamic range, that is they should have a wide range of "power" levels with individual "power" levels that are close together (the NXT motors are pretty good in this respect).
3. Both the sensor and the thing being controlled must respond quickly. "Quick" in this case is "much faster than anything else that is happening in the system". Often when you are controlling motors it isn't possible to get "quick" response since motors take time to react to a change in power. It can take a few tenths of a second for Lego motors to react to a change in power levels. That means the robot's actions are lagging behind the P controller's commands. That makes accurate control difficult with a P controller.

### Adding "I" To The Controller: The PI Controller ("I": what have you done for me lately?)

To improve the response of our P controller we will add a new term to the equation. This term is called the **integral**, the "I" in PID. Integrals are a very important part of advanced mathematics, fortunately the part we need is pretty straight forward.

The integral is the running sum of the error.

Yep, it's that simple. There are a few subtle issues we'll skip for the moment.

Each time we read the light sensor and calculate an **error** we will add that **error** to a variable we will call **integral** (clever eh?).

```
integral = integral + error
```

That equation might look a little odd, and it is. It isn't written as a mathematical statement, it is written in a common form used in programming to add up a series of values. Mathematically it doesn't make any sense. In computer programming the equals sign has a somewhat different meaning than in math. (I'll use the same typewriter font I used for the pseudo code examples to highlight that it is a programming form and not a proper mathematical form.) The "=" means do the math on the right and save the result in the variable named on the left. We want the computer to get the old value of **integral**, add the **error** to it then save the result back in **integral**.

Next, just like the P term, we will multiply the **integral** by a proportionality constant, that's another K. Since this proportionality constant goes with the integral term we will call it **Ki**. Just like the proportional term we multiply the integral by the constant (**Ki**) to get a correction. For our line following robot it is an addition to our **Turn** variable.

```
Turn = Kp*(error) + Ki*(integral)
```

The above is the basic equation for a PI controller. **Turn** is our correction for the motors. The proportional term is **Kp\*(error)** and the integral term is **Ki\*(integral)**.

What exactly does the integral term do for us? If the **error** keeps the same sign for several loops the **integral** grows bigger and bigger. For example, if we check the light sensor and calculate that the **error** is 1, then a short time later we check the sensor again and the **error** is 2, then the next time the **error** is 2 again, then the **integral** will be 1+2+2=5. The **integral** is 5 but the **error** at this particular step is only 2. The integral can be a large factor in the correction but it usually takes a while for the **integral** to build up to the point where it starts to contribute.

Another thing that the integral does is it helps remove small errors. If in our line follower the light sensor is pretty close to the line's edge, but not exactly on it, then the **error** will be small and it will only take a small correction to fix. You might be able to fix that small **error** by changing **Kp** in the proportional term but that will often lead to a robot that oscillates (wobbles back and forth). The **integral** term is perfect for fixing small errors. Since the **integral** adds up the **errors**, several consecutive small **errors** eventually makes the **integral** big enough to make a difference.

One way to think about the **integral** term is that it is the controller's "memory". The **integral** is the cumulative history of the **error** and gives the controller a method to fix errors that persist for a long time.

### Some subtle issues with the integral

Yep, the integral has more detail. Fortunately they aren't too painful.

I glossed over a minor issue (OK, it really isn't minor but we are going to make it so), the time. The integral is really the sum of the **error\*(delta time)**. Delta time (**dT**) is the time between the last time we checked the sensor and the time of the most recent check of the sensor;

```
integral = integral + error*(dT)
```

So every time we add to **integral** the thing we should add is the **error** times the **dT**. It is fairly easy to have the robot measure the **dT**. We would just read a timer each time we read the light sensor. If we subtract the last time from the current time we get the time since the last reading **dT**. (There are better ways to do this but I'll skip'm since they are not needed.) But wouldn't it be nice if didn't have to measure the **dT** and do the multiplication? Well, what if the **dT** is always the same? Every time we add to **integral** we have that same **dT** term. So we can take that factor of **dT** out of **error\*(dT)** and just do the summing the way we did before;

```
integral = integral + error
```

Only when we want to do another calculation with **integral** do we actually need to multiply by **dT**. But wait there's more...

We can do even more to hide the time term. The integral term in the PI controller equation is **Ki\*(integral)\*dT**. But **Ki** is a parameter that we have to fine tune (just like **Kp**) so why not just replace the **Ki\*dT** part with a new **Ki**? The new **Ki** is different from the original but since we don't know either one it doesn't really matter which one we use or what we call it. No matter what we call it or what it represents we still have to find the correct value largely by trial and error.

So we have completely removed the time element for the integral term with the restriction that all the time steps, **dTs**, are the same (or about the same).

### The integral has a memory like an elephant

One last detail should be mentioned about the **integral**. Usually the **integral** can only be moved towards zero, where it doesn't contribute anything to the controller, by having **error** values added that are the opposite sign of most of the ones that we have already collected in **integral**. For example, if over several cycles through the loop the **errors** are 1,2,2,3,2,1

that adds up to an **integral** of 11. But the **error** at the last data point is only 1, which is much smaller than the **integral** at that point. The only way for the **integral** to move towards zero is to get a string of negative **errors** to counter balance the earlier string of positive **errors** to "wind down" the **integral**. For example, if the next few errors are -2,-2,-3 then the integral will drop from 11 to 4 and we would still need more negative **errors** to get the **integral** down to zero. In addition, the **integral** wants the total **error** to be evenly distributed between positive and negative errors.

If something happens that pushes our line following robot to the left of the line's edge the **integral** term not only wants to get back to the line's edge it also wants to overshoot the edge to the right by as much as the original disturbance was the left. So the integral tends to "wind-up" if there are large errors that persist for a while. This can cause problems with controllers that include an **integral** term. Sometimes this tendency of the **integral** term to want to overshoot when it tries to correct the **error** is a big enough problem that the programmer must do something to the **integral** term so it won't cause problems. If **integral** wind-up is a problem two common solutions are (1) zero the **integral**, that is set the variable **integral** equal to zero, every time the **error** is zero or the **error** changes sign. (2) "Dampen" the integral by multiplying the accumulated **integral** by a factor less than one when a new **integral** is calculated. For example;

$$\text{integral} = (2/3)*\text{integral} + \text{error}$$

This reduces the previous integral value by 1/3 each time through the loop. If you think of the integral term as the controllers "memory" then this damping is forcing it to become forgetful of things that happened a "long" time ago.

### Pseudo code for the PI controller

To add the integral term to the controller we need to add a new variable for **Ki** and one for the **integral** itself. And don't forget that we are multiplying our Ks by 100 to help with the integer math restrictions.

```
Kp = 1000           ! REMEMBER we are using Kp*100 so this is really 10 !
Ki = 100           ! REMEMBER we are using Ki*100 so this is really 1 !
offset = 45        ! Initialize the variables
Tp = 50
integral = 0       ! the place where we will store our integral
Loop forever
  LightValue = read light sensor ! what is the current light reading?
  error = LightValue - offset    ! calculate the error by subtracting the offset
  integral = integral + error    ! our new integral term
  Turn = Kp*error + Ki*integral ! the "P term" and the "I term"
  Turn = Turn/100               ! REMEMBER to undo the affect of the factor of 100 in Kp !
  powerA = Tp + Turn            ! the power level for the A motor
  powerC = Tp - Turn            ! the power level for the C motor
  MOTOR A direction=forward power=powerA ! actually issue the command in a MOTOR block
  MOTOR C direction=forward power=powerC ! actually issue the command in a MOTOR block
end loop forever              ! done with this loop, go back to the beginning and do it again.
```

## Adding "D" To The Controller: The Full PID Controller ("D": what is going to happen next?)

Our controller now contains a proportional (P) term that tries to correct the current error and an **integral** (I) term that tries to correct past errors is there a way for the controller to look ahead in time and perhaps try to correct **error** that hasn't even occurred yet?

Yes, and the solution is another concept from advanced mathematics called the **derivative**. Ahhh, there's the "D" in PID. Like the **integral**, the **derivative** can represent some pretty serious mathematics. Fortunately for us, what we need for the PID is fairly simple.

We can look into the future by assuming that the next change in the **error** is the same as the last change in the **error**.

That means the next **error** is expected to be the current **error** plus the change in the **error** between the two preceding sensor samples. The change in the **error** between two consecutive points is called the **derivative**. The **derivative** is the same as the slope of a line.

That might sound a bit complex to calculate but it really isn't too bad. A sample set of data will help illustrate how it works. Lets assume that the current **error** is 2 and the **error** before that was 5. What would we predict the next error to be? Well, the change in error is the **derivative** which is;

$$(\text{the current error}) - (\text{the previous error})$$

which for our numbers is  $2 - 5 = -3$ . The current **derivative** therefore is -3. To use the **derivative** to predict the next **error** we would use

$$(\text{next error}) = (\text{the current error}) + (\text{the current derivative})$$

which for our numbers is  $2 + (-3) = -1$ . So we predict the next **error** will be -1. In practice we don't actually go all the way and predict the next **error**. Instead we just use the **derivative** directly in the controller equation.

The D term, like the I term, should actually include a time element, and the "official" D



term is;

### **Kd(derivative)/(dT)**

Just as with the **proportional** and **integral** terms we have to multiply by a constant. Since this is the constant that goes with the **derivative** it is called **Kd**. Notice also that for the derivative term we divide by **dT** whereas in the **integral** term we had multiplied by **dT**. Don't worry too much about why that is since we are going to do the same kinds of tricks to get rid of the **dT** from the **derivative** term as we did for the **integral** term. The fraction **Kd/dT** is a constant if **dT** is the same for every loop. So we can replace **Kd/dT** with another **Kd**. Since this K, like the previous Ks, is unknown and has to be determined by trial and error it doesn't matter if it is **Kd/dT** or just a new value for **Kd**.

We can now write the complete equation for a PID controller:

$$\text{Turn} = K_p(\text{error}) + K_i(\text{integral}) + K_d(\text{derivative})$$

It is pretty obvious that "predicting the future" would be a handy thing to be able to do but how exactly does it help? And how accurate is the prediction?

If the current **error** is worse than the previous **error** then the D term tries to correct the **error**. If the current **error** is better than the previous **error** then the D term tries to stop the controller from correcting the **error**. It is the second case that is particularly useful. If the **error** is getting close to zero then we are approaching the point where we want to stop correcting. Since the system probably takes a while to respond to changes in the motors' power we want to start reducing the motor power before the **error** has actually gone to zero, otherwise we will overshoot. When put that way it might seem that the equation for the D term would have to be more complex than it is, but it isn't. The only thing you have to worry about is doing the subtraction in the correct order. The correct order for this type of thing is "current" minus "previous". So to calculate the **derivative** we take the current **error** and subtract the previous **error**.

### **Pseudo code for the PID controller**

To add the derivative term to the controller we need to add a new variable for **Kd** and a variable to remember the last **error**. And don't forget that we are multiplying our Ks by 100 to help with the integer math.

```
Kp = 1000           ! REMEMBER we are using Kp*100 so this is really 10 !
Ki = 100           ! REMEMBER we are using Ki*100 so this is really 1 !
Kd = 10000        ! REMEMBER we are using Kd*100 so this is really 100!
offset = 45       ! Initialize the variables
Tp = 50
integral = 0      ! the place where we will store our integral
lastError = 0     ! the place where we will store the last error value
derivative = 0    ! the place where we will store the derivative
Loop forever
  LightValue = read light sensor ! what is the current light reading?
  error = LightValue - offset    ! calculate the error by subtracting the offset
  integral = integral + error    ! calculate the integral
  derivative = error - lastError ! calculate the derivative
  Turn = Kp*error + Ki*integral + Kd*derivative ! the "P term" the "I term" and the "D term"
Turn = Turn/100           ! REMEMBER to undo the affect of the factor of 100 in Kp, Ki and Kd!
powerA = Tp + Turn       ! the power level for the A motor
powerC = Tp - Turn       ! the power level for the C motor
MOTOR A direction=forward power=PowerA ! actually issue the command in a MOTOR block
MOTOR C direction=forward power=PowerC ! same for the other motor but using the other power level
lastError = error        ! save the current error so it can be the lastError next time around
end loop forever         ! done with loop, go back and do it again.
```

We now have the pseudo code for our complete PID controller for a line following robot. Now comes what is often the tricky part, "tuning" the PID. Tuning is the process of finding the best, or at least OK, values for **Kp**, **Ki** and **Kd**.

## **Tuning A PID Controller Without Complex Math (but we still have to do some math)**

Very smart people have already figured out how to tune a PID controller. Since I'm not nearly as smart as they are, I'll use what they learned. It turns out that measurement of couple of parameters for the system allows you to calculate "pretty good" values for **Kp**, **Ki** and **Kd**. It doesn't matter much what the exact system is that is being controlled the tuning equations *almost* always work pretty well. There are several techniques to calculate the Ks, one of is called the "*Ziegler-Nichols Method*" which is what we will use. A google search will locate many web pages that describe this technique in all it's gory detail. The version that I'll use is almost straight from the [Wiki page on PID Controllers](#) (the same treatment is found in many other places). I'll just make one small change by including the loop time (**dT**) in the calculations shown in the table below.

To tune your PID controller you follow these steps:

1. Set the **Ki** and **Kd** values to zero, which turns those terms off and makes the controller act like a simple P controller.
2. Set the **Tp** term to a smallish one. For our motors 25 might be a good place to start.
3. Set the **Kp** term to a "reasonable" value. What is "reasonable"?

1. I just take the maximum value we want to send to the motor's power control (100) and divide by the maximum useable error value. For our line following robot we've assumed the maximum error is 5 so our guess at **Kp** is  $100/5=20$ . When the error is +5 the motor's power will swing by 100 units. When the error is zero the motor's power will sit at the **Tp** level.
2. Or, just set **Kp** to 1 (or 100) and see what happens.
3. If you have implemented that the K's are all entered as 100 times their actual value you have to take that into account here. 1 is entered as 100, 20 as 2000, 100 as 10000.
4. Run the robot and watch what it does. If it can't follow the line and wanders off then increase **Kp**. If it oscillates wildly then decrease **Kp**. Keep changing the **Kp** value until you find one that follows the line and gives noticeable oscillation but not really wild ones. We will call this **Kp** value "**Kc**" ("critical gain" in the PID literature).
5. Using the **Kc** value as **Kp**, run the robot along the line and try to determine how fast it is oscillating. This can be tricky but fortunately the measurement doesn't have to be all that accurate. The oscillation period (**Pc**) is how long it takes the robot to swing from one side of the line to the other then back to the side where it started. For typical Lego robots **Pc** will probably be in the range of about 0.5 seconds to a second or two.
6. You also need to know how fast the robot cycles through it's control loop. I just set the loop to a fixed number of steps (like 10,000) and time how long the robot takes to finish (or have the robot do the timing and display the result.) The time per loop (**dT**) is the measured time divided by the number of loops. For a full PID controller, written in NXT-G, without any added buzzes or whistles, the **dT** will be in the range of 0.015 to 0.020 seconds per loop.
7. Use the table below to calculate a set of **Kp**, **Ki**, and **Kd** values. If you just want a P controller then use the line in the table marked P to calculate the "correct" **Kp** (**Ki** and **Kd** are both zero). If you want a PI controller then use the next line. The full PID controller is the bottom line.
8. If you have implemented that the K's are all entered as 100 times their actual value you don't have to take that into account in these calculations. That factor of 100 is already take into account in the **Kp = Kc** value you determined.
9. Run the robot and see how it behaves.
10. Tweak the **Kp**, **Ki** and **Kd** values to get the best performance you can. You can start with fairly big tweaks, say 30% then try smaller tweaks to get the optimal (or at least acceptable) performance.
11. Once you have a good set of K's try to boost the **Tp** value, which controls the robot's straight speed.
12. Re-tweak the K's or perhaps even go back to step 1 and repeat the entire process for the new **Tp** value.
13. Keep repeating until the robot's behavior is acceptable.

<b>Ziegler-Nichols method giving K' values</b> (loop times considered to be constant and equal to dT)			
<b>Control Type</b>	<b>Kp</b>	<b>Ki'</b>	<b>Kd'</b>
<i>P</i>	$0.50K_c$	0	0
<i>PI</i>	$0.45K_c$	$1.2K_p dT / P_c$	0
<i>PD</i>	$0.80K_c$	0	$K_p P_c / (8dT)$
<i>PID</i>	$0.60K_c$	$2K_p dT / P_c$	$K_p P_c / (8dT)$

The primes (apostrophes) on the **Ki'** and **Kd'** are just to remind you that they are calculated assume **dT** is constant and **dT** has been rolled into the K values.

Here are the values I measured for my test robot (the one in the video linked later on). **Kc** was 300 and when **Kp=Kc** the robot oscillated at about 0.8 seconds per oscillation so **Pc** is 0.8. I measured **Pc** by just counting out loud every time the robot swung fully in a particular direction. I then compared my perception of how fast I was counting with "1-potato -- 2-potato -- 3-potato ...". That's hardly "precision engineering" but it works well enough so we'll call it "practical engineering". The loop time, **dT**, is 0.014 seconds/loop determined by simply running the program for 10,000 loops and having the NXT display the run time. Using the table above for a PID controller we get;

$$\begin{aligned}
 K_p &= (0.60)(K_c) = (0.60)(300) = 180 \\
 K_i &= 2(K_p)(dT) / (P_c) = 2(180)(0.014) / (0.8) = 6.3 \text{ (which is rounded to 6)} \\
 K_d &= (K_p)(P_c) / ((8)(dT)) = (180)(0.8) / ((8)(0.014)) = 1286
 \end{aligned}$$

After further trial and error tuning the final values were 220, 7, and 500 for **Kp**, **Ki** and **Kd** respectively. Remember that all of my K's are entered as 100x their actual value so the actual values are 2.2, 0.07 and 5.

#### **How changes in Kp, Ki, and Kd affect the robots behavior**

The table and method described above is a good starting point for optimizing your PID. Sometimes it helps to have a better idea of what the result will be of increasing (or decreasing) one of the three Ks. The table below is available from many web sites. This particular version is from the Wiki on PID controllers.

<b>Effects of increasing parameters</b>			

Parameter	Rise time	Overshoot	Settling time	Error at equilibrium
$K_p$	Decrease	Increase	Small change	Decrease
$K_i$	Decrease	Increase	Increase	Eliminate
$K_d$	Indefinite (small decrease or increase)	Decrease	Decrease	None

The "Rise Time" is how fast the robot tries to fix an error. In our sample case it is how fast the robot tries to get back to the line edge after it has drifted off of it. The rise time is mostly controlled by  $K_p$ . A larger  $K_p$  will make the robot try to get back faster and decreases the rise time. If  $K_p$  is too large the robot will overshoot.

The "Overshoot" is how far past the line edge the robot tends to go as it is responding to an error. For example, if the overshoot is small then the robot doesn't swing to the right of the line as it is trying to fix being to the left of the line. If the overshoot is large then the robot swings well past the line edge as it tries to correct an error. Overshoot is largely controlled by the  $K_d$  term but is strongly affected by the  $K_i$  and  $K_p$  terms. Usually to correct for too much overshoot you will want to increase  $K_d$ . Remember our first very simple line follower, the one that could do nothing but turn right or left? That line follower has very bad overshoot. Indeed that is about all it does.

The "settling time" is how long the robot takes to settle back down when it encounters a large change. In our line following case a large change occurs when the robot encounters a turn. As the robot responds to the curve it will correct the **error** and then overshoot by some amount. It then needs to correct the overshoot and might overshoot back the other way. It then needs to correct the overshoot ... well, you get the idea. As the robot is responding to an **error** it will tend to oscillate around the desired position. The "settling time" is how long that oscillation takes to dampen out to zero. The settling time responds strongly to both the  $K_i$  and  $K_d$  terms. Bigger  $K_i$  gives longer settling times. Bigger  $K_d$  gives shorter settling time.

"Error at Equilibrium" is the error remaining as the system operates without being disturbed. For our line follower it would be the offset from the line as the robot follows a long straight line. Often P and PD controllers will end up with this kind of error. It can be reduced by increasing  $K_p$  but that may make the robot oscillate. Including an I term and increasing  $K_i$  will often fix a P or PD controller that has a constant error at equilibrium. (This assumes you even care about a small remaining error as the robot follows the line. It just means it is offset to one side or the other by a small amount.)

## How well does it work?

Here's a short video of a basic Lego Mindstorms robot following the line on the test mat that comes with the set. The video quality isn't very good.

The light sensor is about 1/2" above the mat and offset to one side of the robot's center line. The  $T_p$  (target power) was set at 70%. The robot averages about 8 inches per second on this course. The robot is a left hand line follower and is following the inside edge of the oval. The inside edge is a bit harder to follow than the outside edge.



[MPEG4 - MP4 \(644KB\)](#)    [QuickTime - MOV \(972KB\)](#)

Overall the line follower appears to work pretty well. If you watch the video closely you'll see the robot "wag its tail" a bit as it comes off the corners. That's the PID oscillating a little. When the robot is running towards the camera you can see the red spot on the mat from the light sensor's LED. It looks to be tracking the line's edge pretty well.

The basic PID controller should work for many different control problems, and of course can be used as a P or PI controller instead of a PID. You would need to come up with a new definition of the **error** and the PID would have to be tuned for the particular task.

## So where's the code?

I could give it to you but then I'd have to kill you.

Since this document is targeted at older FLL kids, I really don't want to give'm the code. They should be able to write their own.

The pseudo code has pretty much everything you need for the PID itself. You may have to add some setup code and perhaps a suitable way of stopping the line follower loop.

As a little bit of help here's a MyBlock that takes two inputs, the target power **Tp** and the **Turn** value, and controls the two motors. This MyBlock also properly deals with negative power levels. It even beeps when a motor reverses directions, which is handy for tuning. A properly tuned line following PID should rarely have to reverse motor directions.

[PID\\_LF\\_MotorControl.rbt](#) is the RBT file for NXT-G v1.1. A screen shot of the program is at [PID\\_LF\\_MotorControl.png](#)

If you would really like to get my PID NXT-G code send me an email.

## Random stuff that might be stuffed into this document someplace

For an excellent example of another PID controller on a Mindstorms robot see [Philos balancing segway like robot](#). The PID is written in NQC ("not quite C"). Balancing is a much trickier control problem than is following a line. ( I know because I've tried it! )

A PID (or PI or P) controller is an example of a *feedback loop*. Feedback is the greatest thing since sliced pickles.

There are advanced methods for tuning a PID controller. Usually it requires hardware and/or software that a Lego robot builder doesn't have.

Some PID controllers are much easier to tune than others. For example, a PID controller is often used to control the temperature in an oven. This is a fairly easy tuning job since the oven is pretty stable, though it may be far from it's target temperature, even when the PID is poorly tuned. PID controllers are also used to control balancing robots. That is much more difficult to tune since the PID has to be tuned pretty well otherwise the robot just falls over. It is hard to tune the PID if the robot promptly falls over every time it is turned on.

There are variants of the Ziegler–Nichols method and other methods for tuning a PID.

There are controllers that are more complex than a PID.

PIDs have been around for a long time and preceded computer control. A PID can, and often has, been implemented in purely mechanical systems. That is, no computer or even any electrical parts.

It would be interesting to have the NXT-G program write data to a file while the PID is running. You would then transfer the data back to the PC for analysis. This would be a great way to determine **Pc**. I believe version 2.0 of NXT-G can transfer data back to the PC in real time for graphing. Writing to a data file (or sending the data via Bluetooth) does have some problems when used with a PID. Writing to a file is a pretty slow process so the PID's loop time will increase, I would think transmitting anything via Bluetooth is also pretty slow. That means the PID takes longer to loop and you are measuring the error and updating the motors less often. Another problem with writing to a file is that periodically the file write routine takes a big chunk of time (as much as 0.1 seconds) to do some "housekeeping". This can be avoided by "pre-extending" the file to the limit when the file is first opened. A NXT-G file can be as big as 32K if you have that much free space on the NXT-G. If you try to pre-extend the data file and you don't have enough memory the NXT-G gives no indication that there was a problem. If you use a method like this then the **Pc** value you obtain is relevant only to the particular **dT** that the "PID with logging" program has. If you want to measure the **Pc** and then remove the data logging code from the program to make it loop faster, the **Pc** is no longer valid. One partial solution is to force all loops of the PID to take the same amount of time. At the beginning of the loop set a timer to zero. At the end of the loop WAIT for a length of time longer than the loop's normal **dT**. You can use this technique to keep the loop times constant even if you add or remove large chunks of code (like data logging). Of course, that means you always have the PID looping slower than it could be, and you are wasting time in each loop cycle.

I've fiddled a bit with writing data to a file while the PID is running. It is handy to start the data file with a listing of the **Tp**, **offset**, **Kp**, **Ki** and **Kd** values. Good data to log each time the PID loop is executed is the time, **error**, PID output and the angle of one of the motor axles. From that data you can reconstruct the integral and derivative so they don't need to be logged.

It is unclear to me just how fast the PID needs to cycle, that is how small **dT** needs to be, to get a good controller. I suspect that the PID needs to cycle faster than the response time of the motors. Perhaps several times faster. Cycling the PID much faster than that probably doesn't help much since things are not changing that fast. The response time of the NXT motors, when they are actually moving a robot, is in the range of a couple of tenths of a second. The PID should probably cycle in say 1/5 to 1/10th that time, or about 0.010 to 0.030 seconds per loop. The basic PID program described above has a **dT** of about 0.015 seconds, which should be fast enough. If the the program also logs data as it runs then the **dT** rises to about 0.030 seconds per loop.

Using raw light values (0 to 1023 scale), instead of uncalibrated light values, might increase the dynamic range of the light sensors. For our example light values black would be 400 and white 500. The **offset** would be 450 with a range of +/-50 instead of +/-5. The raw light values is available from a data port on the light sensor block. If you calibrate your light sensor under your lighting conditions and use the calibrated values then white will be about 100 and black will be about 0. This is another way to increase the proportional range of the light sensor. In both the raw and calibrated modes the light values probably are not accurate in the last digit but hopefully the values are somewhat more precise than

using a light value range of just 10 or so.

When creating a PID controller there is often a couple different ways to define the error. For our line follower the error is proportional to how far the sensor is from the line's edge. The derivative is how fast the sensor is moving towards, or away from, the line's edge. The integral is sum of the distances from the line's edge, which really doesn't have much physical significance (though it does still help the controller). There are other ways to do things. We could define the error as how fast we are moving towards or away from the line's edge. In other words, the error is now what was the derivative in our line follower. For this new definition of error, the derivative becomes how fast we are accelerating towards, or away from, the line's edge. The integral becomes how far we are from the line's edge, which does make physical sense. Which method works best often depends on how accurate you can measure the error and how much noise (random fluctuation) there is. If we use the velocity as the error, it has to be calculated from the light reading and is the derivative of the light reading. To get the derivative for the PID we have to take the derivative of a derivative. The derivative of a derivative probably won't work very well with our limited proportional range of light values.

For the "three level line follower" the three ranges don't need to be the same size. If this type of follower is good enough then it is often better to make the center range larger than the two outer ranges. Something like 42 to 47 perhaps for our example values. The only thing you have to worry about is that this becomes pretty sensitive to small changes in the room lighting. The three even ranges (and the original two range approach) are fairly insensitive to changes in the room lighting. If you make the center range too large you run the risk of having a small change in room lighting move your light range outside what you expected. The light sensor might never return numbers in either the lowest or highest range and the robot will never turn in one of the two directions.

#### **Some realities of PIDs.**

1. When the error goes out of the proportional range the derivative goes to zero.
2. The derivative is sensitive to noise.
3. The derivative works best when the error precision is high. For our line follower the error is an integer between -5 and +5. That's pretty poor precision. Perhaps use the derivative of the motors' axle velocity instead?

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